

Unification of the standard model and dark matter sectors in $[\text{SU}(5) \times \text{U}(1)]^4$

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ABSTRACT: A simple model of dark matter contains a light Dirac field charged under a hidden $\text{U}(1)$ gauge symmetry. When a chiral matter content in a strong dynamics satisfies the t'Hooft anomaly matching condition, a massless baryon is a natural candidate of the light Dirac field. One realization is the same matter content as the standard $\text{SU}(5) \times \text{U}(1)_{(B-L)}$ grand unified theory. We propose a chiral $[\text{SU}(5) \times \text{U}(1)]^4$ gauge theory as a unified model of the SM and DM sectors. The low-energy dynamics, which was recently studied, is governed by the hidden $\text{U}(1)_4$ gauge interaction and the third-family $\text{U}(1)_{(B-L)_3}$ gauge interaction. This model can realize self-interacting dark matter and alleviate the small-scale crisis of collisionless cold dark matter in the cosmological structure formation. The model can also address the semi-leptonic B -decay anomaly reported by the LHCb experiment.

KEYWORDS: Cosmology of Theories beyond the SM, GUT

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1 Introduction

A simple framework of dark matter (DM) consists of a light Dirac fermion charged under a new $U(1)$ gauge symmetry. The $U(1)$ symmetry, which is spontaneously broken to some discrete group at low energy, ensures the stability of the light Dirac fermion. Annihilation of the light Dirac fermions into the gauge bosons determines its thermal relic to be consistent with the observed DM abundance. Here, one may ask a couple of questions: why is the Dirac fermion light?; and what is the origin of the $U(1)$ gauge boson? Since the Dirac mass term is allowed by any symmetries, it is mysterious that the mass of Dirac field is as light as, e.g., the electroweak scale.

We can naturally realize the DM framework based on a chiral $SU(5)$ gauge theory that becomes strong at some intermediate scale. We introduce two chiral “preons” whose representations are $\bar{\mathbf{5}}$ and $\mathbf{10}$, which are analogous to the minimal $SU(5)$ grand unified theory (GUT) of the standard model (SM). Around 1970s, there were a lot of efforts to identify quarks and leptons as composite states of preons [1–6]. In this context, t’Hooft showed that the anomaly matching condition must be satisfied when there is a massless composite fermion at low energy [7]. Although nobody has found a viable theory for composite quarks and leptons, ref. [8] found that $\bar{\mathbf{5}}$ and $\mathbf{10}$ in a strong $SU(5)$ dynamics results in a massless fermion. There is a gauge-anomaly-free global $U(1)$ symmetry, which

is analogous to the $U(1)_{B-L}$ symmetry in the SM $SU(5)$ GUT. The $[U(1) \text{ graviton}]^2$ and $[U(1)]^3$ anomalies at high energy and at low energy match.¹ By introducing a Dirac partner of the massless fermion, which is analogous to the right-handed neutrino, we gauge the $U(1)$ symmetry. A dimension 6 operator among those fermions at a high-energy scale results in a Dirac mass term below the dynamical scale. The mass scale is of order the electroweak scale when the operator is suppressed by the Planck scale and the dynamical scale is of order 10^{13} GeV. Therefore, we naturally obtain a light Dirac fermion and a $U(1)$ gauge interaction at low energy from the $SU(5) \times U(1)$ gauge theory.

When the gauge boson is lighter than the $U(1)$ -breaking Higgs, the gauge boson is stable and harmful in cosmology. A kinetic mixing with some other gauge boson makes it decay to SM particles. On the other hand, if the kinetic mixing also makes late-time annihilation of DM Dirac fermions result in high-energy electromagnetic particles, it is tightly constrained by high-energy cosmic-ray experiments and observations of cosmic microwave background anisotropies (i.e., indirect detection experiments). These problems are evaded when the hidden $U(1)$ gauge boson kinetically mixes only with the third-family $U(1)_{(B-L)}$ (i.e., $U(1)_{(B-L)_3}$) [12]. When the hidden $U(1)$ gauge boson mass is below the tau lepton mass, it dominantly decays to third-family neutrinos.

The above observation motivates us to consider a flavored GUT $[SU(5) \times U(1)]^4$. Three SM families are charged under the different $SU(5)_i \times U(1)_i$ ($i = 1, 2, 3$). We identify the chiral $SU(5)_4 \times U(1)_4$ gauge theory as the DM sector. The first three pairs of gauge symmetries are spontaneously broken into the SM gauge symmetries and the last one becomes strong at an intermediate scale to give the SIDM model (see figure 1).

Low-energy phenomenology has been studied in ref. [12]. The $U(1)_4$ gauge symmetry is assumed to be spontaneously broken at 10–100 MeV. The $U(1)_4$ gauge boson can mediate a strong self-interaction of DM. Self-interacting dark matter (SIDM) may alleviate tensions of collisionless DM in the small-scale structure formation (see, e.g., ref. [13] for a review of SIDM). For example, SIDM can explain the diversity of galactic rotation curves [14–16], while it is not easy for collisionless DM [17] (see, e.g., ref. [18] for a review of the small-scale crisis). The self-interaction mediated by the light $U(1)_4$ gauge boson is strong at low velocities, but is weakened at high velocities so that it evades constraints from observations of galaxy clusters [19] (see refs. [20–29] for SIDM models in a similar direction). Furthermore, the $U(1)_{(B-L)_3}$ gauge boson and flavor mixing, e.g., through the vector-like fermions [30], introduces a new contribution to semi-leptonic Wilson coefficients. It can explain the lepton flavor-universality violation in semi-leptonic B meson decays recently reported by the Belle experiment [31, 32] and LHCb experiment [33–35] (see also updated analysis in terms of semi-leptonic Wilson coefficients [36–39]).

This paper is organized as follows. In the next section, we briefly explain the simple model of DM. The model can realize SIDM to address the small-scale crisis of collisionless

¹Generically, N anti-fundamentals and one antisymmetric tensor in a strong $SU(4 + N)$ dynamics leave $N(N + 1)/2$ massless composite fermions. The massless fermions may be identified as right-handed neutrinos [9]. See ref. [10] for an application of a similar idea to the Peccei-Quinn mechanism. A model of DM from a strong $SU(5)$ gauge theory was discussed in ref. [11], although vector-like pairs of preons are introduced.

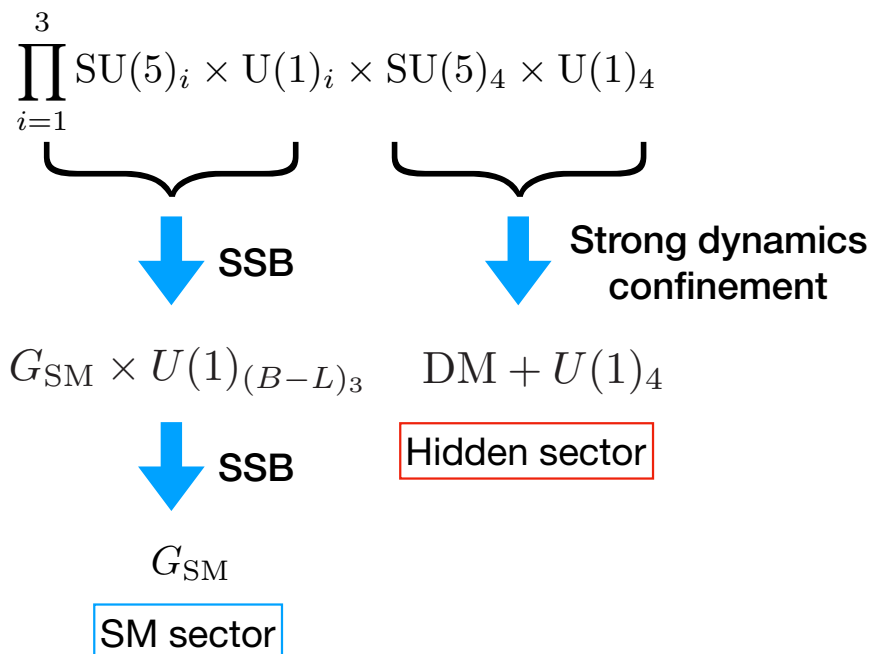


Figure 1. Gauge symmetry breaking pattern in our unified model. The SM gauge group is denoted as $G_{\text{SM}} = \text{SU}(3)_c \times \text{SU}(2)_L \times \text{U}(1)_Y$.

DM. The model can also explain the B-decay anomaly. In section 3, we demonstrate that the SM sector as well as the DM sector can be unified in four copies of a $\text{SU}(5) \times \text{U}(1)$ gauge dynamics. The simple low-energy model of DM can be naturally obtained from the strong dynamics of the high-energy $\text{SU}(5)_4 \times \text{U}(1)_4$ gauge theory. We specify the bosonic particle content and breaking pattern of $\text{SU}(5)_i \times \text{U}(1)_i$ ($i = 1, 2, 3$) into the SM to see that the gauge couplings are unified at a high scale. We conclude in section 4.

2 Low-energy model

In this section we briefly review a simple framework of DM introduced in ref. [12]. The low-energy model is based on $\text{U}(1)_{(B-L)_3} \times \text{U}(1)_4$ extension of the SM model. In particular we put stress on that the flavored $\text{U}(1)_{(B-L)_3}$ symmetry is needed, which leads us to introduce $\prod_{i=1}^3 [\text{SU}(5)_i \times \text{U}(1)_i]$. We also briefly describe a mechanism to reproduce the observed flavor mixing. We assume that the flavor structure is generated by a set of TeV-scale vector-like fermions introduced for each SM fermion (including the right-handed neutrinos).

2.1 Simple framework of DM

In a simple DM framework, we introduce a Dirac field η (DM) charged under a hidden gauge symmetry $\text{U}(1)_4$.² The Lagrangian density in the DM sector is given by

$$\mathcal{L}_h = (\text{kinetic terms}) - m_\eta \bar{\eta} \eta - V_{\Phi_4}(\Phi_4), \quad (2.1)$$

²In ref. [12], χ and $\text{U}(1)_h$ denote η and $\text{U}(1)_4$, respectively.

where Φ_4 is a Higgs field that spontaneously breaks $U(1)_4$ into some discrete group. This discrete group stabilizes the Dirac field η . Annihilation of η into the $U(1)_4$ gauge boson Z_4 leads to thermal freeze-out of η and determines the relic abundance. Z_4 also mediates the velocity-dependent self-interaction of η . If the $U(1)_4$ is spontaneously broken at 10–100 MeV, the self-scattering cross section is large enough at low velocities to alleviate the small-scale crisis of collisionless DM. Meanwhile, its cross section is small enough to evade constraints from galaxy clusters.

If Z_4 is stable, its relic abundance will overclose the Universe. To make it decay, we introduce the $U(1)_{(B-L)_3}$ gauge symmetry and a kinetic mixing between the gauge boson $Z_{(B-L)_3}$ and Z_4 :

$$\mathcal{L}_3 = (\text{kinetic terms}) - \left(\frac{1}{2} y_3 \Phi_3 N_3 N_3 + \text{h.c.} \right) - V_{\Phi_3}(\Phi_3) - \frac{1}{2} \epsilon_2 F_{4\mu\nu} F_{(B-L)_3}^{\mu\nu}, \quad (2.2)$$

where F 's are the field strengths of the corresponding gauge bosons. N_3 is the third-family right-handed neutrino and Φ_3 is a Higgs field that breaks $U(1)_{(B-L)_3}$ spontaneously. If the Z_4 mass is below the tau lepton mass, only the decay channel of Z_4 into the third-family neutrinos is kinematically allowed. Indirect detection bounds on DM are systematically weakened because DM annihilation mainly result in neutrinos. A kinetic mixing between the hypercharge gauge boson Z_Y and $Z_{(B-L)_3}$ is also induced by SM-particle loops:

$$\mathcal{L}_{Y-(B-L)_3} = -\frac{1}{2} \epsilon_1 F_{Y\mu\nu} F_{(B-L)_3}^{\mu\nu}. \quad (2.3)$$

The kinetic mixing leads to observable signals in direct and indirect detection experiments of DM [12].

2.2 Flavor structure and leptogenesis

Although it is forbidden by the flavored symmetries $U(1)_{(B-L)_i}$ ($i = 1, 2, 3$), the proper structure of the Yukawa interactions in the SM sector is expected to be induced from their spontaneous symmetry breakings. We assume that these $U(1)_{(B-L)_i}$ are spontaneously broken by vacuum expectation values (VEVs) v_i of Higgs fields Φ_i . We consider that v_3 is at the TeV scale so that the $U(1)_4$ gauge boson can efficiently decay into neutrinos via the kinetic mixing ϵ_2 . We also assume that v_1 and v_2 are of order 10^9 GeV so that we can realize the seesaw mechanism to explain the small but nonzero masses of SM neutrinos [40–43] and the thermal leptogenesis via the decay of the first and second-family right-handed neutrinos N_1 and N_2 [44] (see, e.g., refs. [45–48] for recent reviews). We also need another set of vector-like fermions above the v_1 and v_2 scales to obtain the Yukawa interactions between the first and second families.

The SM Yukawa matrices can be diagonalized by a unitary rotation for each fermion: $f = U_f f'$ ($f = u_L, d_L, u_R, d_R, \nu_L, l_L, l_R$). In the mass eigenstate, the interactions with the $Z_{(B-L)_3}$ gauge boson are then given by

$$\mathcal{L} \supset - \sum_f g_{(B-L)_3} Q_f Z_{(B-L)_3}^\mu J_{f,\mu}, \quad (2.4)$$

$$J_{f,\mu} = \sum_{i,j=1}^3 \bar{f}_i (U_f)_{3i}^* (U_f)_{3j} \gamma_\mu f_j, \quad (2.5)$$

where Q_f is a $U(1)_{(B-L)_3}$ charge of fermion f . As a result, $Z_{(B-L)_3}$ mediates interactions between different families in the mass eigenstate. It is beyond the scope of this paper to study the possible structure of U_f . Ref. [12] assumes that the CKM and PMNS matrices are attributed to u_L and ν_L , respectively. It is also assumed that an additional family rotation can appear only between the second and third families. Under the existence of the additional rotation, the Z_4 mass should be smaller than the muon mass so that its decay into muons is kinematically prohibited. An additional family rotation between the first and third generation should be minuscule to prohibit Z_4 from significantly decaying into electrons.

The additional family rotation between the second and third families leads to interesting phenomenology in collider physics. In particular, we can explain the semi-leptonic B meson decays recently reported by the LHCb experiment [33, 34], consistently with other collider events, like $D^0-\bar{D}^0$ mixing and $\tau \rightarrow 3\mu$ [12] (see also ref. [30]). A benchmark point, where all collider constraints as well as the DM constraints are evaded, is $\alpha_{(B-L)_3} = 10^{-4}$, $\alpha_4 = 10^{-3}$, $m_{Z_{(B-L)_3}} = 70 \text{ GeV}$, $m_{Z_4} = 10 \text{ MeV}$, $m_\eta = 40 \text{ GeV}$, $\epsilon_1 = 10^{-2}$, and $\epsilon_2 = 4 \times 10^{-2}$.

3 High-energy model

In this section, we explain our unified model for the SM and DM sectors. There remain a question unanswered in the low-energy DM model described in the previous section: why a DM Dirac field is light? and where the almost unbroken $U(1)_4$ symmetry originate? First, we see that a chiral $SU(5)_4 \times U(1)_4$ gauge theory in the DM sector answers these questions. Then, motivated by the flavored symmetry, we introduce a $\prod_{i=1}^3 [SU(5)_i \times U(1)_i]$ gauge theory in the SM sector. We study the symmetry breaking pattern and gauge coupling unification. Finally, we end up with a $[SU(5) \times U(1)]^4$ gauge theory in a unified model of the SM and DM sectors.

3.1 DM sector from a $SU(5)_4 \times U(1)_4$ GUT

Let us introduce chiral $SU(5)_4$ dynamics with $\bar{\mathbf{5}}$ and $\mathbf{10}$ representations $\psi_4(-3)$ and $\chi_4(1)$ (i.e., preons). The parentheses denote the charges under global $U(1)$ symmetry, which we denote as $U(1)_4$ and is not anomalous with the gauge (except for gravity) symmetries. We assume that the $SU(5)_4$ gauge interaction becomes strong and is confined below an intermediate scale Λ . At low energy, there is a chiral baryon composed of three fermions as

$$\eta \equiv \psi_4 \psi_4 \chi_4. \tag{3.1}$$

The $U(1)_4$ charge of this baryon state is -5 . One can check that η satisfies the t'Hooft anomaly matching condition of $[U(1)_4 \text{ graviton}]^2$ and $[U(1)_4]^3$. Thus η can be massless.³

³It is also possible that the $U(1)_4$ is dynamically broken by the condensate of $(\psi_4 \psi_4 \chi_4)^2$. In this paper, we assume that the condensation scale of operators that break $U(1)_4$ is sufficiently small so that Z_4 gauge boson mass can be as light as the electroweak scale.

	ψ_i	χ_i	N_i
$SU(5)_i$	$\bar{\mathbf{5}}$	$\mathbf{10}$	$\mathbf{1}$
$U(1)_i$	-3	1	5

Table 1. Fermionic field (matter) content ($i = 1, 2, 3, 4$).

Since we want to have DM coupled to a light gauge boson, we promote the $U(1)_4$ symmetry to a gauge symmetry.⁴ Once we promote it to the gauge symmetry, we have a gauge anomaly, such as $[U(1)_4]^3$. However, it is easy to cancel the anomaly by introducing a Dirac partner of the η , which is denoted by N_4 . This is nothing but the chiral fermion called the right-handed neutrino in the SM sector. It is surprising that the matter content in this $SU(5)_4 \times U(1)_4$ sector is completely the same as that of the standard $SU(5) \times U(1)_{B-L}$ model. Here we note that the following non-renormalizable operator is allowed by the gauge symmetries:

$$\frac{c}{M_{\text{Pl}}^2} N_4 \psi_4 \psi_4 \chi_4 + \text{h.c.}, \tag{3.2}$$

where we expect a constant c to be of order unity. This gives a Dirac mass for η and N_4 ($\equiv \bar{\eta}$) of order $\Lambda^3/M_{\text{Pl}}^2$.⁵ If $\Lambda = 10^{13}$ GeV, the Dirac mass is around the electroweak scale. This Dirac field is identified as DM discussed in section 2.1.

3.2 SM sector from a $[SU(5) \times U(1)]^3$ GUT

In a similar way as the minimal $SU(5)$ GUT, we introduce a $\prod_{i=1}^3 [SU(5)_i \times U(1)_i]$ theory with $\bar{\mathbf{5}}$ and $\mathbf{10}$ representations ψ_i and χ_i ($i = 1, 2, 3$). We also introduce the right-handed neutrinos N_i charged only under $U(1)_i$. The charge assignment for these fermions is summarized in table 1. One can check again that these gauge interactions are free from quantum anomaly.

$SU(5)_i$ ($i = 1, 2, 3$) are assumed to be spontaneously broken into the diagonal subgroup of $SU(3)_c \times SU(2)_L \times U(1)_Y$.⁶ The $U(1)_i$ symmetry can be identified as $U(1)_{(B-L)_i}$ ($i = 1, 2, 3$) by taking a linear combination with $U(1)_Y$. In the following, we study the breaking pattern and gauge coupling unification. They are non-trivial because there are many ways to spontaneously break the $\prod_{i=1}^3 SU(5)_i$ gauge group into the SM gauge group and there may be light fields that affect the renormalization group running of the gauge couplings. We explain one specific scenario that can realize the gauge coupling unification.

⁴If the $U(1)_4$ symmetry is just global, quantum gravity effects may induce a Majorana mass to η . Although the Majorana mass may be minuscule since it arises from a dimension 9 operator, it is better that we avoid it by gauging the $U(1)_4$ symmetry.

⁵If the charge of the $U(1)_4$ breaking Higgs Φ_4 is -10 in analogy to that of $U(1)_{B-L}$, the Majorana mass of order its VEV v_4 is introduced to N_4 . The introduced mass splitting between DM states changes the DM phenomenology (see, e.g., ref. [28]) from the pure Dirac case studied in ref. [12], where the $U(1)_4$ charge of Φ_4 is three times that of η .

⁶This part is similar to a $[SO(10)]^3$ GUT [30, 49].

We note that we do not assume supersymmetry⁷ nor try to address the doublet-triplet splitting for the Higgs field in this paper. We therefore expect that fine-tuning problems can be addressed by some unknown mechanism or may not be a problem at all in quantum field theories. In this context, it may be reasonable to assume that there are some light fields much below the GUT scale in addition to the SM Higgs doublet.

We introduce bifundamental scalars Ω_{ij} ($i \neq j$; $\Omega_{ij} = \Omega_{ji}^*$) and adjoint scalars Σ_i in addition to Higgs fields H_i . The charge assignment of these scalar fields is summarized in table 2. Since there can be many terms in the scalar potential, we do not give details of the scalar potential. $\prod_{i=1}^3[\text{SU}(5)_i]$ are spontaneously broken by the VEVs of Ω_{ij} and Σ_i as

$$\langle \Omega_{ij} \rangle = \text{diag} (a_{ij}, a_{ij}, a_{ij}, b_{ij}, b_{ij}) , \tag{3.3}$$

$$\langle \Sigma_i \rangle = c_i \cdot \text{diag} (1/3, 1/3, 1/3, -1/2, -1/2) , \tag{3.4}$$

where $a_{ij} \neq b_{ij}$. Here we note that $\langle \Omega_{ij} \rangle$ does not need to be traceless. In particular, either a_{ij} or b_{ij} can be zero at least at an intermediate scale. There are several ways to spontaneously break $\prod_{i=1}^3[\text{SU}(5)_i]$ into the SM group G_{SM} . In the rest of this section, we consider the following sequence of the spontaneous symmetry breakings as an example:

$$\prod_{i=1}^3 [\text{SU}(5)_i] \rightarrow [\text{SU}(3)]^2 \times \text{SU}(2)_L \times \text{U}(1)_Y \rightarrow \text{SU}(3)_c \times \text{SU}(2)_L \times \text{U}(1)_Y . \tag{3.5}$$

We denote the energy scales of the first and second spontaneous symmetry breakings as E_{GUT} and $E_{\text{SU}(3)}$ ($\ll E_{\text{GUT}}$), respectively. This can be realized when a_{12} , b_{12} , and b_{23} are about E_{GUT} , while a_{23} is about $E_{\text{SU}(3)}$.⁸ A further discussion on the scalar potential is given in appendix A. We denote $[\text{SU}(3)]^2$ at the intermediate scale as $\text{SU}(3)_d \times \text{SU}(3)_3$, where $\text{SU}(3)_d$ is a diagonal subgroup of $\text{SU}(5)_1 \times \text{SU}(5)_2$ and $\text{SU}(3)_3$ is a subgroup of $\text{SU}(5)_3$. In this example, the colored bifundamental $\Omega_{c,31}$ from Ω_{31} spontaneously breaks $\text{SU}(3)_d \times \text{SU}(3)_3$ at $E_{\text{SU}(3)}$. The Yukawa interactions between the first and second families can be introduced at E_{GUT} .⁹

We note that the renormalizable potential (e.g., $\text{Tr}[\Omega_{12}\Omega_{23}\Omega_{31}]$) accidentally respects global relative-phase rotations among Ω_{ij} . However, they can be explicitly broken by dimension 5 operators like $\text{Det}[\Omega_{ij}]$. The associated pseudo-NG bosons are therefore much heavier than the electroweak scale and are decoupled from the low-energy physics. We assume that one of the mass eigenstate among the Higgs doublets $H_{L,i}$ is at the electroweak scale so that we can spontaneously break $\text{SU}(2)_L \times \text{U}(1)_Y$ down to $\text{U}(1)_{\text{em}}$.

As commented in section 2.2, there should be a non-trivial field content at the TeV scale to reproduce a correct Yukawa structure. Following ref. [30], we consider that there

⁷If the theory respects supersymmetry at a high energy scale, it should be spontaneously broken above 10^{13} GeV so that it does not affect the strong dynamics of $\text{SU}(5)_4$. We note that the supersymmetry may improve the gauge coupling unification without adjoint scalars Ψ_i .

⁸We note that all of a_{ij} and b_{ij} do not need to have a nonzero VEV to break $[\text{SU}(5)]^3$ into the SM group. Here we assume that a_{31} (b_{31}) is smaller than a_{12} and a_{23} (b_{12} and b_{23}) or zero.

⁹Here we implicitly assume that $\text{U}(1)_i$ ($i = 1, 2$) are spontaneously broken at the same scale for simplicity. If the $\text{U}(1)_i$ breaking scale is lighter, the set of vector-like multiplets of $\text{SU}(5)_i$ should also be lighter to produce the Yukawa interactions between the first and second families. Since they form complete multiplets of $\text{SU}(5)_i$, they do not spoil the unification of the gauge couplings.

	$\Omega_{ij} = \Omega_{ji}^*$	H_i	Ψ_i	Σ_i	Φ_i
$SU(5)_i$	$\bar{\mathbf{5}}$	$\bar{\mathbf{5}}$	$\mathbf{24}$	$\mathbf{24}$	$\mathbf{1}$
$SU(5)_j$	$\mathbf{5}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$
$U(1)_i$	0	2	0	0	-10

Table 2. Scalar field content ($i, j = 1, 2, 3$ and $i \neq j$).

is a set of vector-like fermions introduced for each SM fermion at the TeV scale. We also need another set of vector-like fermions above the $U(1)_i$ ($i = 1, 2$) breaking scale to obtain the Yukawa interactions between the first and second families. Assuming a universality of particle contents in the ultraviolet physics for $SU(5)_i$ ($i = 1, 2, 3$), we introduce three sets of vector-like multiplets that are $\mathbf{5} + \bar{\mathbf{5}}$ and $\mathbf{10} + \bar{\mathbf{10}}$ representations under $SU(5)_i$, respectively. Only one set of vector multiplets should be at the TeV scale. We identify it as that charged under $SU(5)_3$.

Dotted lines in figure 2 depict the runnings of the gauge couplings. We summarize details on the runnings of the gauge couplings in appendix B. At $E_{\text{GUT}} \simeq 2 \times 10^{13}$ GeV, the gauge group is spontaneously broken to $SU(3)_d \times SU(3)_3 \times SU(2)_L \times U(1)_Y$. Then $SU(3)_d \times SU(3)_3$ gauge group is spontaneously broken to $SU(3)_c$ at $E_{SU(3)} \simeq 5 \times 10^{11}$ GeV. However, our model predicts proton decay that is mediated by the heavy gauge fields. The mass scale of the gauge fields is of order $E_{\text{GUT}} \simeq 2 \times 10^{13}$ GeV, which is so low that the model is excluded by the constraint on the proton decay rate.

To evade the constraint, we introduce three adjoint scalars for $SU(3)_c$ and $SU(2)_L$, $\Psi_{c,i}$ and $\Psi_{L,i}$ ($i = 1, 2, 3$), at 10 TeV. They make the GUT scale larger than that without these fields [50]. We expect that these fields originate from three scalar fields with the adjoint scalars Ψ_i . The resulting runnings of the gauge couplings are shown as the solid lines in figure 2. The GUT scale is now given by $E_{\text{GUT}} \simeq 2 \times 10^{16}$ GeV and the $SU(3)_d \times SU(3)_3$ breaking scale is given by $E_{SU(3)} \simeq 6 \times 10^{14}$ GeV. The GUT scale is high enough to evade the constraint on the proton decay rate.

The decay of the additional adjoint fields, which we denote as $\Psi_{L,i}$ and $\Psi_{c,i}$, does not cause a cosmological problem. We can write operators like $\Psi_{L,i} H_{L,i}^\dagger H_{L,i}$ and $\Psi_{c,i} H_{c,i}^\dagger H_{c,i}$, where $H_{c,i}$ are colored Higgs fields. The $SU(2)_L$ adjoint fields $\Psi_{L,i}$ decay fast into the SM Higgs field by the former operator. The $SU(3)_c$ adjoint fields $\Psi_{c,i}$ decay into quarks via one-loop effect, which is suppressed by the mass of colored Higgs field. Since the mass of the colored Higgs fields can be as light as 10^{12} GeV,¹⁰ to evade the constraint on the proton decay rate, the $SU(3)_c$ adjoint field can decay long before the big bang nucleosynthesis epoch.

Before closing the section, we briefly comment on another simple possibility to realize the gauge coupling unification in our model. If the $\prod_{i=1}^3 SU(5)_i$ gauge group is spontaneously broken into the SM gauge group at a single energy scale, we can use a scenario of gauge coupling unification for the standard $SU(5)$ GUT. One simple example was proposed in ref. [51], where we introduced leptoquarks and a $\bar{\mathbf{5}}$ Higgs field at the TeV scale to realize

¹⁰Light colored Higgs fields changes the running of the gauge couplings only slightly.

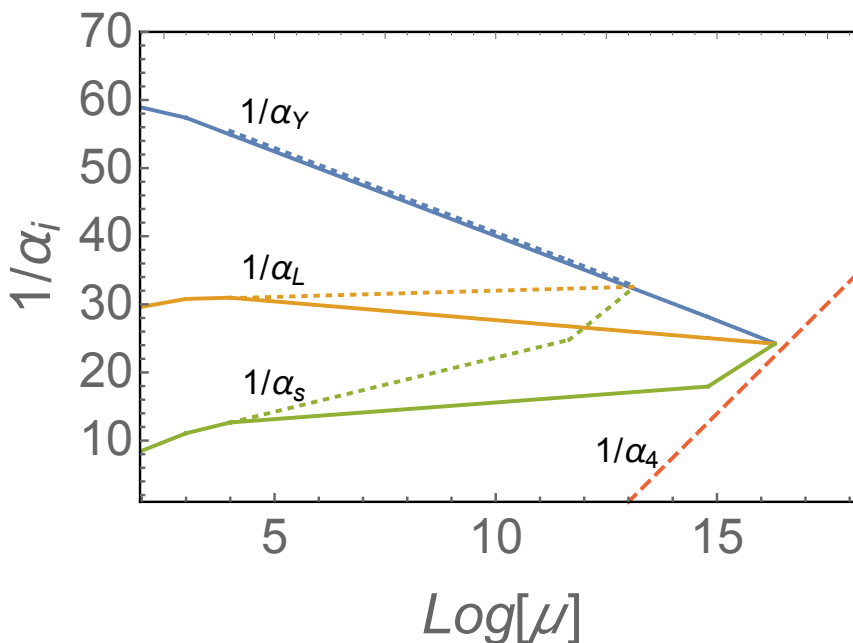


Figure 2. Renormalization group runnings of the gauge couplings with (solid lines) and without (dotted lines) adjoint fields $\Psi_{L,i}$ and $\Psi_{c,i}$ at 10 TeV. The renormalization scale μ is in units of GeV. The dashed line represents the running of α_4^{-1} . At the energy scale between $E_{\text{SU}(3)}$ and E_{GUT} , we plot $\alpha_s^{-1} = \alpha_{\text{SU}(3)_d}^{-1} + \alpha_{\text{SU}(3)_3}^{-1}$ as an effective coupling that should match the $\text{SU}(3)_c$ at $E_{\text{SU}(3)}$.

the gauge coupling unification. Although the GUT scale of this model is too low, we can make it high enough by introducing adjoint fields for $\text{SU}(2)_L$ and $\text{SU}(3)_c$ [50].

3.3 $[\text{SU}(5) \times \text{U}(1)]^4$ unified model

So far we discuss a $\prod_{i=1}^3 [\text{SU}(5)_i \times \text{U}(1)_i]$ ($i = 1, 2, 3$) theory in the SM sector and a $\text{SU}(5)_4 \times \text{U}(1)_4$ theory in the DM sector. It is surprising that the fermion content in each $[\text{SU}(5)_i \times \text{U}(1)_i]$ ($i = 1, 2, 3, 4$) is identical to each other. In figure 2, we can see that all $\text{SU}(5)_i$ gauge couplings are of the same order, which may indicate that all $\text{SU}(5)_i$ gauge groups are unified at a higher scale. We end up with a unified chiral $[\text{SU}(5) \times \text{U}(1)]^4$ theory with the identical gauge couplings. We would like to emphasize that the DM mass is predicted to be of order 100 GeV in this unified theory. The unified gauge coupling is usually in the range of $1/20$ – $1/25$ and the GUT scale is about 10^{16} GeV in most reasonable GUT models. The dynamical scale of the fourth $\text{SU}(5)_4$ gauge theory is then of order 10^{13} GeV because of the running of the gauge coupling from the GUT scale. As a result, the mass of DM is then naturally at the TeV scale from the dimension 6 operator. The DM mass being predicted is an outstanding feature. Here we would remember the reason why weakly interacting massive particles (WIMPs) have been attractive. This is because its mass is predicted at the TeV scale so that TeV-scale new physics solves the naturalness problem. Thus, we could say that our DM candidate is as compelling (and miraculous) as traditional WIMPs.

4 Conclusion

We have proposed a chiral $\prod_{i=1}^4 [\text{SU}(5)_i \times \text{U}(1)_i]^4$ gauge theory as a unified model of the SM and DM sectors. The chiral matter content in each $\text{SU}(5) \times \text{U}(1)$ sector is the same as that of the standard $\text{SU}(5)$ GUT. The first three sets of $\text{SU}(5)$ gauge groups are spontaneously broken into a diagonal subgroup, which is identified as the SM gauge group. The first two $\text{U}(1)$ gauge symmetries are also spontaneously broken at a high-energy scale, while the third one is spontaneously broken at the TeV scale. We have provided an example of the particle content that realizes the gauge coupling unification around 10^{16} GeV.

The fourth $\text{SU}(5)$ gauge interaction becomes strong at $\Lambda \sim 10^{13}$ GeV, when its gauge coupling strength is identical to that of the first three sets of $\text{SU}(5)$ (i.e., the visible GUT) at the GUT scale. A chiral baryon state satisfies the t'Hooft anomaly matching condition below the confinement scale. The baryon and the $\text{U}(1)_4$ charged fermion form a Dirac field whose mass, arising from a dimension 6 operator, is of order $\Lambda^3/M_{\text{Pl}}^2 = 1$ TeV. This Dirac field is identified as a dominant component of DM. In other words, we have found that the model naturally predicts the DM mass of order the electroweak scale from the running of the unified gauge coupling. Since the unified gauge coupling as well as the GUT scale do not change much in viable GUT scenarios, this is a universal prediction of our model.

The low-energy phenomenology is studied in ref. [12]. The $\text{U}(1)_4$ gauge symmetry is spontaneously broken at low energy into some discrete group, which stabilizes the DM Dirac field. Thermal freeze-out through annihilations into the $\text{U}(1)_4$ gauge bosons reproduces the correct DM abundance. The $\text{U}(1)_4$ gauge boson also mediates the DM self-interaction. In particular, when the $\text{U}(1)_4$ gauge symmetry is spontaneously broken at 10–100 MeV, the strength and velocity dependence of the self-interaction can be consistent with that indicated by the small-scale crisis of collisionless DM in the cosmological small-scale structure formation.

We need to introduce the kinetic mixing between $\text{U}(1)_4$ and $\text{U}(1)_{(B-L)_3}$ gauge boson so that the unwanted $\text{U}(1)_4$ gauge boson dominantly decays into the third-family neutrino. Through the loop-induced kinetic mixing between the $\text{U}(1)_{(B-L)_3}$ and $\text{U}(1)_Y$ gauge bosons, still, it can decay into electrons although it is subdominant. It leads to a detectable signal in the indirect detection experiment of DM. The kinetic mixings also predict observable signals in the direct detection experiment of DM. In addition, the lepton flavor-universality violation of semi-leptonic B meson decays reported by the LHCb experiment can be explained by the $\text{U}(1)_{(B-L)_3}$ gauge boson with an additional second-third family mixing.

Finally, we comment on the issues that we have solved and have not solved in the specific realization of the $[\text{SU}(5) \times \text{U}(1)]^4$ GUT described in this paper. As we mentioned above, the specific realization of the $[\text{SU}(5) \times \text{U}(1)]^3$ GUT do not solve any fine-tuning problem inherited in the minimal $\text{SU}(5)$ GUT of the SM, like the hierarchy problem, the doublet-triplet splitting problem, and inclusion of light particles to achieve the gauge coupling unification. We regard the specific realization as a proof of concept and expect that these issues are solved by some unknown mechanism or may not be physical problems at all. On the other hand, we are driven by the intriguing fact that the theory similar to the minimal $\text{SU}(5) \times \text{U}(1)$ GUT of the SM naturally reproduces the low-energy simple

framework of DM. The model explains the existence of light DM, its abundance, small-scale issues of collisionless cold dark matter in cosmological structure formation, and the B-decay anomaly.

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A More on the scalar potential

In this appendix, we give a further discussion on the scalar potential.

A.1 GUT breaking at hierarchical scales

We consider the symmetry breaking pattern of eq. (3.5) with hierarchical scales in the main text. $[\text{SU}(5)]^3$ is broken into $[\text{SU}(3)]^2 \times \text{SU}(2)_L \times \text{U}(1)_Y$ at E_{GUT} and then into the SM gauge group at $E_{\text{SU}(3)}$ ($\ll E_{\text{GUT}}$).

We consider the potential of Ω_{ij} such as

$$V_\Omega = \sum_{\substack{(i,j)= \\ (1,2),(2,3),(1,3)}} (M_{ij}^2 \text{Tr} [\Omega_{ij} \Omega_{ji}] + \lambda_{ij} \text{Tr} [\Sigma_i \Omega_{ij} \Sigma_j \Omega_{ji}] + \lambda'_{ij} \text{Tr} [(\Omega_{ij} \Omega_{ji})^2]) , \quad (\text{A.1})$$

where we omit the other renormalizable terms for the sake of notational simplicity. First, the adjoint scalars Σ_i develop VEVs of eq. (3.4) as in the standard $\text{SU}(5)$ GUT model. These break $[\text{SU}(5)]^3$ down to $[\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)]^3$. The of Ω_{ij} can be rewritten as the effective potential for a_{ij} and b_{ij} defined in eq. (3.3):

$$V(a_{ij}) = \sum_{\substack{(i,j)= \\ (1,2),(2,3),(1,3)}} 3 [M_{ij,a}^2 a_{ij}^2 + \lambda'_{ij} a_{ij}^4] , \quad (\text{A.2})$$

$$V(b_{ij}) = \sum_{\substack{(i,j)= \\ (1,2),(2,3),(1,3)}} 2 [M_{ij,b}^2 b_{ij}^2 + \lambda'_{ij} b_{ij}^4] , \quad (\text{A.3})$$

where

$$M_{ij,a}^2 = M_{ij}^2 + \frac{\lambda_{ij} c_i c_j}{9} , \quad (\text{A.4})$$

$$M_{ij,b}^2 = M_{ij}^2 + \frac{\lambda_{ij} c_i c_j}{4} . \quad (\text{A.5})$$

It is possible that $M_{12,a}^2 < 0$, $M_{12,b}^2 < 0$, $M_{23,a}^2 > 0$, $M_{23,b}^2 < 0$, $M_{31,a}^2 < 0$, $M_{31,b}^2 > 0$. Then a_{23} and b_{31} are zero while a_{12} , b_{12} , b_{23} , and a_{31} have nonzero values. We assume

that a_{12} , b_{12} , and b_{23} are about the GUT scale, E_{GUT} , while a_{31} is about $E_{\text{SU}(3)}$, which is orders of magnitude smaller than E_{GUT} . This can be realized by taking $|M_{31,a}^2| \ll |M_{12,a}^2|, |M_{12,b}^2|, |M_{23,b}^2|$ by tuning a parameter. In this example, $[\text{SU}(5)]^3$ (or $[\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)]^3$) is broken into $\text{SU}(3) \times \text{SU}(3) \times \text{SU}(2)_L \times \text{U}(1)_Y$ at E_{GUT} and then into the SM gauge group at $E_{\text{SU}(3)}$.

A.2 GUT breaking at a single scale

We can also consider that $[\text{SU}(5)]^3$ is broken to the SM gauge group at a single scale, while we do not consider it in the main text. In this case, we do not need to introduce the adjoint scalars Σ_i . The general potential of Ω_{ij} is given by

$$\begin{aligned}
 V_\Omega = & \sum_{\substack{(i,j)= \\ (1,2),(2,3),(1,3)}} M_{ij}^2 \text{Tr} \left[|\Omega_{ij}|^2 \right] + (A \text{Tr} [\Omega_{12} \Omega_{23} \Omega_{31}] + \text{h.c.}) \\
 & + \sum_{\substack{(i,j,k,l)= \\ (1,2,1,2),(2,3,2,3),(3,1,3,1), \\ (1,2,1,3),(2,3,2,1),(3,1,3,2)}} \lambda_{ijkl} \text{Tr} \Omega_{ij} \Omega_{jk} \Omega_{kl} \Omega_{li} + \sum_{\substack{(i,j),(k,l)= \\ (1,2),(2,3),(1,3)}} \lambda_{ij,kl} \text{Tr} |\Omega_{ij}|^2 \text{Tr} |\Omega_{kl}|^2,
 \end{aligned}
 \tag{A.6}$$

where M_{ij} are components of a mass matrix, $A > 0$ is a parameter with mass dimension one, and λ_{ijkl} are quartic coupling constants.

Although the explicit values of these VEVs are quite complicated, we write them for the case of an universal $\lambda_{ijkl} (\equiv \lambda)$ and $\lambda_{ij,kl} = 0$ in units of $M_{ij}^2 = -c^2$ as an illustration. We consider

$$\langle \Omega_{ij} \rangle = \text{diag} (a_{ij}^1, a_{ij}^2, a_{ij}^3, a_{ij}^4, a_{ij}^5), \tag{A.7}$$

and find

$$\begin{aligned}
 a_{12}^k = a_{23}^k = a_{31}^k, \quad a_{12}^k = -a_{23}^k = -a_{31}^k, \quad -a_{12}^k = a_{23}^k = -a_{31}^k, \quad \text{or} \\
 -a_{12}^k = -a_{23}^k = a_{31}^k = -\frac{c}{8\lambda} \left(A + \sqrt{A^2 + 16\lambda} \right),
 \end{aligned}
 \tag{A.8}$$

for $k = 1, 2, 3, 4, 5$. There are degenerate vacua with $\text{SU}(5)$, $\text{SU}(4) \times \text{U}(1)$, or $\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$, which are diagonal subgroups of $\text{SU}(5)_1 \times \text{SU}(5)_2 \times \text{SU}(5)_3$.

B Runnings of gauge couplings

In this section, we summarize the one-loop beta function coefficients b_i ($i = 1, 2, 3, 4$) used in figure 2:

$$\frac{dg_i}{d \ln \mu} = \frac{b_i}{16\pi^2} g_i^3. \tag{B.1}$$

The beta function coefficient of the gauge coupling for $\text{SU}(5)_4$ is given by

$$b_4 = -\frac{11}{3} \cdot 5 + \frac{2}{3} \cdot \left(\frac{1}{2} + \frac{3}{2} \right) = -\frac{51}{3}. \tag{B.2}$$

We assume that the dynamical scale of $SU(5)_4$ is of order 10^{13} GeV so that the Dirac mass eq. (3.2) is around the electroweak scale. The resulting renormalization group running for α_4 is shown in figure 2 as the dotted line.

At the energy scale between $E_{SU(3)}$ and E_{GUT} , the beta function coefficients of the gauge couplings are as follows:

$$\frac{5}{3}b_{U(1)_Y} = \frac{2}{3} \cdot (3+2) \cdot \left(6 \cdot \frac{1}{36} + 3 \cdot \frac{4}{9} + 3 \cdot \frac{1}{9} + 2 \cdot \frac{1}{4} + 1\right) + \frac{1}{3} \cdot \left(2 \cdot \frac{1}{4}\right) = \frac{203}{18}, \quad (B.3)$$

$$b_{SU(2)_L} = -\frac{11}{3} \cdot 2 + \frac{2}{3} \cdot (3+2) \cdot \left(3 \cdot \frac{1}{2} + \frac{1}{2}\right) + \frac{1}{3} \cdot \left(\frac{1}{2}\right) = -\frac{1}{2}, \quad (B.4)$$

$$b_{SU(3)_d} = -\frac{11}{3} \cdot 3 + \frac{2}{3} \cdot 2 \cdot \left(2 \cdot \frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right) + \frac{1}{3} \cdot \left(3 \cdot \frac{1}{2}\right) = -\frac{47}{6}, \quad (B.5)$$

$$b_{SU(3)_3} = -\frac{11}{3} \cdot 3 + \frac{2}{3} \cdot (1+2) \cdot \left(2 \cdot \frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right) + \frac{1}{3} \cdot \left(3 \cdot \frac{1}{2}\right) = -\frac{13}{2}. \quad (B.6)$$

Here, we take into account the bifundamental scalar $\Omega_{c,31}$ that spontaneously breaks $SU(3)_d \times SU(3)_3$ to $SU(3)_c$ at $\mu = E_{SU(3)}$.

Below $E_{SU(3)}$ but above the TeV scale, the beta function coefficients are given by

$$\frac{5}{3}b_{U(1)_Y} = \frac{2}{3} \cdot (3+2) \cdot \left(6 \cdot \frac{1}{36} + 3 \cdot \frac{4}{9} + 3 \cdot \frac{1}{9} + 2 \cdot \frac{1}{4} + 1\right) + \frac{1}{3} \cdot \left(2 \cdot \frac{1}{4}\right) = \frac{203}{18}, \quad (B.7)$$

$$b_{SU(2)_L} = -\frac{11}{3} \cdot 2 + \frac{2}{3} \cdot (3+2) \cdot \left(3 \cdot \frac{1}{2} + \frac{1}{2}\right) + \frac{1}{3} \cdot \left(\frac{1}{2}\right) = -\frac{1}{2}, \quad (B.8)$$

$$b_{SU(3)_c} = -\frac{11}{3} \cdot 3 + \frac{2}{3} \cdot (3+2) \cdot \left(2 \cdot \frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right) = -\frac{13}{3}, \quad (B.9)$$

where the running is modified by the presence of the vector-like multiplets when compared to the SM.

The junction conditions of the gauge couplings are given by

$$\alpha_Y^{-1} = \alpha_L^{-1} = \sum_{i=1}^3 \alpha_i^{-1}, \quad (B.10)$$

$$\alpha_{SU(3)_d}^{-1} = \sum_{i=1}^2 \alpha_i^{-1}, \quad (B.11)$$

$$\alpha_{SU(3)_3}^{-1} = \alpha_3^{-1}, \quad (B.12)$$

at $\mu = E_{GUT}$ and

$$\alpha_s^{-1} = \alpha_{SU(3)_d}^{-1} + \alpha_{SU(3)_3}^{-1}, \quad (B.13)$$

at $\mu = E_{SU(3)}$. At the energy scale between $E_{SU(3)}$ and E_{GUT} , we plot the running of α_Y^{-1} , α_L^{-1} , and $\alpha_{SU(3)_d}^{-1} + \alpha_{SU(3)_3}^{-1}$. Because of the junction conditions, all of them must be unified at $\mu = E_{GUT}$ and the last combination of the gauge couplings is continuously connected to α_s^{-1} at $\mu = E_{SU(3)}$.

We introduce three adjoint scalars for $SU(3)_c$ and $SU(2)_L$, $\Psi_{c,i}$ and $\Psi_{L,i}$ ($i = 1, 2, 3$), at the 10 TeV scale to make E_{GUT} higher. They change the beta function coefficients as follows. At the energy scale between $E_{SU(3)}$ and E_{GUT} ,

$$b'_{SU(2)_L} = b_{SU(2)_L} + \frac{1}{3} \cdot 3 \cdot (2) , \tag{B.14}$$

$$b'_{SU(3)_d} = b_{SU(3)_d} + \frac{1}{3} \cdot 2 \cdot (3) , \tag{B.15}$$

$$b'_{SU(3)_3} = b_{SU(3)_3} + \frac{1}{3} \cdot (3) . \tag{B.16}$$

Below $E_{SU(3)}$ but above the TeV scale,

$$b'_{SU(2)_L} = b_{SU(2)_L} + \frac{1}{3} \cdot 3 \cdot (2) , \tag{B.17}$$

$$b'_{SU(3)_c} = b_{SU(3)_c} + \frac{1}{3} \cdot 3 \cdot (3) . \tag{B.18}$$

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