Magnetoelectric octahedral breathing mode in the ferrimagnetic La$_2$CoIrO$_6$ double perovskite

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Distortion of transition-metal ion-oxygen octahedra in perovskite structure has been a long standing subject for exploring the physics of charge-orbital–spin-lattice couplings. Recent findings in nickelates or BaBiO$_3$ have suggested that a charge disproportionation in the transition-metal ions can evoke certain cooperative breathing distortions (CBD), constituted by the symmetric expansion and shrinkage of the octahedra in contrast to the Jahn-Teller-type asymmetric distortion. A double perovskite ferrimagnet, La$_2$CoIrO$_6$ bears inherently the charge disproportionation in the cationic sites with Co$^{2+}$ and Ir$^{4+}$ sublattices. In light of seeking the clues for the CBD and its coupling to the magnetic order, the crystal structure and magnetic structure of La$_2$CoIrO$_6$ were examined at various temperatures by using neutron diffraction. Structure refinements and mode decomposition analyses revealed that, indeed, a CBD mode exists substantially in La$_2$CoIrO$_6$ while preserving the symmetry of the octahedral distortion is the Jahn-Teller distortion, that is, O$_6$’s are distorted asymmetrically (like an elongation in one of B-O bond direction) as in LaMnO$_3$ [7] or La$_{0.75}$Ca$_{0.25}$MnO$_3$ [8].

I. INTRODUCTION

Perovskite-type transition-metal oxides have been widely studied in condensed-matter researches since there have been observed a variety of emergent phenomena including, for instance, colossal magnetoresistance, multiferroicity [1], and photocatalysis [2]. In most cases of the perovskite oxides, such functionalities originate from a complex interplay among charge, orbital, spin, and lattice degrees of freedom of $d$ electrons [1]. Therefore, it is of significant interest to identify the possible orders in those degrees of freedom and their correlation.

In the case of perovskites $ABO_3$ (typically, $A$ is an alkali-metal or rare-earth ion and $B$ is a transition-metal ion), the corner-sharing $BO_6$ octahedra can be distorted or rotate cooperatively depending on the sizes of $A$ and $B$ ions, which is well characterized by the Goldschmidt tolerance factor [1] and 15 Glazer tilting systems [3–6]. The most well-known type of the octahedral distortion is the Jahn-Teller distortion, that is, $BO_6$’s are distorted asymmetrically (like an elongation in one $B$-O bond direction) as in LaMnO$_3$ [7] or La$_{0.75}$Ca$_{0.25}$MnO$_3$ [8].

On the other hand, certain octahedral distortion that can preserve symmetry in $BO_6$’s has been also observed in some materials having charge inhomogeneity. For instance, alternatingly mixed Bi$^{3+}$ and Bi$^{5+}$ ions (rather than Bi$^{4+}$) in BaBiO$_3$ ($Fm\overline{3}m$) resulted in doubling of all the lattice constants of the aristo-type cubic $ABO_3$ ($Pm\overline{3}m$) [9], and the charge disproportionation $2Ni^{3+} \rightarrow Ni^{3+} + Ni^{3-} + Ni^{3-} + Ni^{3-}$ in $R$NiO$_3$ ($R$: rare-earth ions except La) induced a structural evolution from $Pbmn(a^{-}a^{-}c^{-})$ to $P2_1/n(a^{-}a^{-}c^{+})$ [10–12]. The two $B$ ions with distinct oxidation numbers are not identical so that a cooperative expansion shrinkage of the $BO_6$ pair, called the cooperative octahedral breathing (CBD) mode, is allowed crystallographically.

The CBD mode can be more prevalent in a double perovskite of $A_2B'B''O_6$ [$Fm\overline{3}m$ ($a^{0}a^{0}a^{0}$)] [6,13–16] since $B$ and $B'$ sites are now fundamentally distinct. Thus the double perovskite system can be an ideal playground for exploring and controlling the CBD modes. Since the discovery of the half-metallic ferrimagnet Sr$_2$FeMoO$_6$ [17], double perovskites with various compositions have been synthesized and characterized in light of enhancing the magnetism for spintronics applications [14]. Regarding the CBD, Solovyev pointed out that the atomic position of the oxygen ions can affect the ferrimagnetism in the double perovskites of Sr$_2$FeMoO$_6$ and Sr$_2$FeReO$_6$ [18]. Also, a Raman

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spectroscopy study substantiated an $A_{1g}$ mode (related to the dynamics of the CBD-type vibration) in contrast to an $E_g$ mode (related to the dynamics of Jahn-Teller-type vibration) in $\text{Ba}_2\text{FeReO}_6$ [19]. However, precise determination on the atomic positions and the information on the mode decomposition in regard to CBD are still lacking.

This paper reports precise information on the cooperative octahedral distortion/rotation in $\text{La}_2\text{CoIrO}_6$ obtained by time-of-flight (t.o.f.) neutron powder diffraction. This material is a ferrimagnet with an antiferromagnetic coupling between Co spins ($\Delta_{CO} = 3/2$; Co$^{2+}$, high-spin configuration) and Ir pseudospins ($\Delta_{\text{eff, Ir}} = 1/2$; Ir$^{4+}$, 5$d^5$) and the Curie temperature ($T_C$) is $\sim 95$ K [20–27]. It was shown that the octahedrally coordinated Co$^{2+}$ with a high-spin configuration as in CoO can have a substantial unquenched angular moment, implying strong spin-orbit-lattice coupling [28]. Furthermore, the octahedrally coordinated Ir$^{4+}$ with strong spin-orbit entanglement effect (as in the representative iridates of $\text{Sr}_2\text{IrO}_4$ [29] or $\text{Na}_2\text{IrO}_3$ [30] can induce exotic Kitaev-Heisenberg magnetism [30] rather than the classical Néel-type antiferromagnetism as in $\text{Li}_2\text{MnO}_3$ [31]. Therefore, possible magnetoelastic (ME) effects can be maximized under the composition. Indeed, we found a signature of strong positive correlation between the CBD mode and the magnetic moment in the composition. Many studies on iridate compounds have been reported, but here we report on the ME coupling with magnetic long-range order in an iridate compound.

II. EXPERIMENTAL METHODS

A $\text{La}_2\text{CoIrO}_6$ powder sample was prepared by solid-state reaction method [23]. The t.o.f. neutron powder diffraction was carried out on $\sim 4$ g of the specimen in the SuperHRPD beamline in J-PARC [32,33]. As shown in the Supplemental Material [34], the 90-deg bank in the end station of the beamline can collect the data with the $Q$ value up to $Q_{\text{max}} = 10.5$ Å$^{-1}$, high enough to study the ME coupling; the errors in the Ir-O bond length are displayed in Fig. S3 in comparison to previous structural studies [20,24].

The space group and lattice structures are directly determined from the t.o.f. values of the diffraction patterns from the 90-deg bank data. The atomic coordinates and the bond lengths, e.g., Ir-O bond lengths or Co-O-Ir bond angles, were obtained by processing the Rietveld refinement using Fullprof [35]. For the magnetic structure analyses, the data were collected from the 30-deg bank and the symmetry analyses were performed employing the SARAH program [36]. The crystal symmetry remained as $P2_1/n$ for all the temperature range, while the details in the atomic positions and spin orders vary with temperature. The complex evolution in the atomic positions under $P2_1/n$ symmetry was interpreted in terms of the tilting and distortion of the IrO$_6$ and CoO$_6$ octahedra compared to the case of aristo-type $Fm\overline{3}m$ ($a^0a^0a^0$) by using the Bilbao crystallographic server [37,38] and ISODISPLACE [39]. (See Ref. [34] for more details.)

III. RESULTS

Figure 1 shows the crystal structure and magnetic structure of $\text{La}_2\text{CoIrO}_6$ at $T = 23$ K determined by neutron powder diffraction. It is shown that the crystal structure possesses the space group of $P2_1/n$ with Glazer tilting notation of $a^- a^+ c^+$ for all the $T$ ranges below room temperature. Results of x-ray-diffraction analyses (Fig. S1 in Ref. [34]) also support the assignment. Figures 1(a) and 1(b) show the top view and the perspective view of the crystal structure, respectively. Co and Ir occupy Wyckoff 2$c$ and 2$d$ positions respectively, both of which have two identical sites: Co atoms are at $(x, y, z) = (0, 1/2, 0)$ and $(1/2, 0, 1/2)$, and Ir atoms are at $(x, y, z) = (1/2, 0, 0)$ and $(0, 1/2, 1/2)$. A possible antisite disorder replacing $B$(Co) with $B'$(Ir) ions was considered in the Rietveld refinement. By adding one more parameter of mixing ratio, the goodness of the fit was improved but only slightly; the $R_{\text{wp}}$ value is reduced from 5.35 to merely 5.08% for a 9% mixing of Co ↔ Ir. Thus we judge that the effects of such antisite disorder are negligible in this compound, as is consistent with a previous report [20].

The magnetic propagation vector $k$ was estimated to be $(0, 0, 0)$, indicating that the magnetic unit cell is identical with the crystal unit cell. The magnetic basis vectors according to the magnetic symmetry analysis are summarized in Table I. There are two possible magnetic models under the magnetic propagation vector group of $2/m$. One is $\Gamma_1(A_y)$, which dictates that if a Co ion has a magnetic moment of $(M_x, M_y, M_z)$ (each of the components is defined as the projection to the lattice vector $a$, $b$, or $c$) the other Co ion in the same unit cell should have a moment of $(-M_x, M_y, -M_z)$; that is, the components of the two Co ions along the $a$ or $c$ axis should be consistent with the previous report [20].

![Figure 1](image-url)
ordered antiferromagnetically, while the components along the b axis should be ordered ferromagnetically. The other model is $\Gamma_1(B_y)$, in which the two Co ions possess $(M_x, M_y, M_z)$ and $(-M_x, -M_y, M_z)$, i.e., ferromagnetic ordering along the a or c axis but antiferromagnetic ordering along the b axis. The requirement for Ir ions is the same as that for Co ions.

According to the results of the magnetic structure analyses for the low-$T$ data, the $\Gamma_1(A_y)$ model reproduces the experimental diffraction patterns much more accurately than the $\Gamma_1(B_y)$ model (see Fig. 6). Therefore, we judge that magnetic structure in La$_2$CoIrO$_6$ has $\Gamma_1(A_y)$ symmetry. The spin alignments according to the symmetry are depicted in Figs. 1(a) and 1(b). The magnetic moment of Co ions at $T = 23$ K was estimated to be $M_{Co} = (A_x, F_y, A_z) = (1.0, 1.7, 1.4) \mu_B$ so that the magnitude $|M_{Co}|$ is 2.4 $\mu_B$, $\sim$80% of the ideal value for high-spin Co$^{2+}$ (3 $\mu_B$) [23].

Meanwhile, the magnetic moment of Ir ions was estimated to be much smaller ($M_{Ir} \ll 0.5 \mu_B$) [22] and indeterminate within the precision of the Rietveld analyses due to strong neutron absorption of Ir ions. The small value of the Ir moment possibly originates from the nature of the spin-orbital entanglement of the $J_{eff}$ state in Ir$^{4+}$ ions [40]. Namely, the expectation value of net spin/ angular moment in the $J_{eff}$ state would be a third of a single spin because the $J_{eff} = 1/2$ state in Ir$^{4+}$ comprises a combination of three t$_{2g}$ orbitals with two spin-up states and one spin-down state [41]. Also, the low precision is contributed mainly by the significant neutron absorption of Ir ions [42] which reduces the magnetic peak intensities for the region of larger d’s to hinder the determination of the weak Ir magnetic moments.

In fact, it can be inferred from the results of previous studies that the Ir magnetic moments ($\sim 0.38 \mu_B$) are aligned antiparallel to the adjacent Co magnetic moments [22]. Previous bulk measurement reported that La$_2$CoIrO$_6$ undergoes a second-order magnetic transition with a single $T_C$ [20,21,23–26]. According to the Landau theory on continuous phase transition, the single transition temperature suggests that Co and Ir sublattices should have the same magnetic irreducible representations (see Table I). Therefore, as for the magnetic structure, considering the alignments of Co magnetic moments only is sufficient for identifying the magnetic structure $[\Gamma_1(A_y)]$.

Examination of the atomic coordinates using the Rietveld analyses shows the correlation between the atomic positions and the ferrimagnetic order. It shows that the oxygen ions move in accordance with the Co magnetic moments as to enlarge or shrink the CoO$_6$ and IrO$_6$ octahedra cooperatively. As $T$ decreases, the O ions in the $ab$ plane (O1 and O2) move by $\sim 0.02$ Å toward adjacent Ir ions so as to enlarge the CoO$_6$ octahedra and shrink the IrO$_6$ octahedra, while the O ions move along c axis (O3) counteractively only by a smaller amount ($<0.01$ Å). (See Fig. 2 for more details.)

The mode decomposition analysis (Appendix C) shows that among the several collective oxygenic movements only the CBD mode, shown by the arrows in Fig. 1(a), is correlated with the values of the magnetic moment (mainly at T's below $T_C$ found in Figs. 3 and 4). This suggests strong ME coupling. Namely, the CBD mode becomes severe as an increasing function of $M_{Co}$ (and resultantly $M_{Ir}$ as well). Figure 1(e) demonstrates the ME coupling in the networks of the CoO$_6$ and IrO$_6$ octahedra. The occupied Co t$_{2g}$ and Ir $J_{eff} = 1/2$ orbitals (lobes and spins (arrows) are displayed schematically. The CBD modes emerge and are enhanced abruptly (but continuously) with decreasing $T (T > T_C \rightarrow T \lesssim T_C \rightarrow T \ll T_C)$. At $T > T_C$, the spin directions are randomly fluctuating because the thermal energy exceeds the threshold energy of the spin order. In contrast, at $T \lesssim T_C$, the spins tend to align in their preferred orientations but with a limited coherence length, and at T’s far below $T_C$ finally all the spins reach the ground-state symmetry of $\Gamma_1(A_y)$. The orbital angular momenta would tend to align parallel or antiparallel due to the spin-orbit coupling effect, and thus the lobes appear to be perpendicular to the arrows (spins) in Fig. 1(c).
The lattice parameters, bond lengths, and bond angles are displayed as functions of $T$ in Fig. 2 and listed in Table II. The lattice parameters of (a) the unit-cell volume ($V$), (b) the lattice constants in a pseudocubic notation [$a_{pc} = (a/\sqrt{2}, b/\sqrt{2}, c/2)$], and (c) the angle $\beta$ of the monoclinic structure were determined by the t.o.f. peak positions and the systematic absence of peaks. Anomalies are shown at $T$'s near $T_C$, suggesting a ME coupling. The theoretical Debye-Gruneneisen (DG) fit is appended in Fig. 2(a) to quantitatively show the volume expansion due to thermal lattice vibrations [43,44]. It is shown that the $V$'s at the low $T$'s are smaller than expected by the DG fit, suggesting the shrinkage of the unit cell in accordance with the magnetic order.

Figures 2(d)–2(g) show, respectively, the bond lengths of Ir-O, Co-O, and Co-Ir ($d_{Co-O}$, $d_{Co-O}$, and $d_{Co-Ir}$), and the Co-O-Ir bond angles ($\angle_{Co-O-Ir}$), obtained by the Rietveld refinement. The average bond lengths of (Ir-O) and (Co-O) are appended in the respective figures. Interestingly, Ir-O bonds are shorter than Co-O bonds overall in spite of the much larger atomic number of Ir. This can be attributed mainly to the high oxidation number of Ir (+4) compared to Co (+2); the bond length decreases significantly as the electron cloud shrinks with less valence electrons. As discussed in Fig. 1, at $T < T_C$, Ir-O1 and Ir-O2 shrink ($\sim-0.02$ Å) while Ir-O3 slightly elongates so that (Ir-O) (empty squares) decreases slightly as $T$ decreases. In contrast, Co-O1 and Co-O2 elongate ($\sim+0.02$ Å) while Co-O3 slightly shrinks so that (Co-O) (empty squares) increases slightly as $T$ decreases. Meanwhile, the Co-Ir bond lengths and Co-O-Ir bond angles barely change ($<0.002$ Å and $<0.5^\circ$) with $T$, at $T < T_C$. This suggests that O1's and O2's (in the ab plane) move toward adjacent Ir sites significantly whereas O3's (along the c axis) move counteractively but only slightly. Therefore, we can infer certain collective distorsion of the CoO$_6$ and IrO$_6$ octahedra.

IV. DISCUSSION

In order to scrutinize the relevance of the structural orders to the ferrimagnetic order, three representative structural order parameters are plotted together with the intensity of the “magnetic” (100)/(010) peak in Fig. 3. The (100)/(010) peaks are observed only at $T < T_C$. (See Fig. 5). Under $P2_1/n$ crystal symmetry, the (100)/(010) reflection from nuclei is forbidden in principle. Indeed, it is not observed in the x-ray-diffraction data for all the $T$ range (Fig. S1 in Supplemental Material [34]). Therefore, the (100)/(010) peak should originate from the magnetic scattering form factors, and their (areal) intensity $I_{mag}$ can be regarded as a measure of strength of the magnetic ordering. The values of $I_{mag}$'s are obtained after subtracting the constant background around the magnetic peak.

Figure 3 shows the $T$ evolution of the volume anomaly $\Delta V = V_{DG} - V_{Exp}$, that is, the magnitude of deviation from the DG fit, the off-center movement of O1 toward Ir ($[d_{Co-O1,d_{Ir-O1}}]/2$), together with the values of $I_{mag}$'s. It is clearly shown that the two structural order parameters strikingly show a very similar $T$ evolution to $I_{mag}$'s. For comparison, the distances between the cations ($d_{Co-Ir}$) are attached...
TABLE II. Results of the Rietveld refinement on the 90-deg bank data.

<table>
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<th>Temperature (K)</th>
<th>280 K</th>
<th>190 K</th>
<th>100 K</th>
<th>90 K</th>
<th>80 K</th>
<th>63 K</th>
<th>46 K</th>
<th>35 K</th>
<th>23 K</th>
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<td>5.5756(1)</td>
<td>5.5712(1)</td>
<td>5.5708(1)</td>
<td>5.5702(1)</td>
<td>5.5693(1)</td>
<td>5.5688(1)</td>
<td>5.5687(1)</td>
<td>5.5684(1)</td>
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<td>(b) ((\AA))</td>
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<td>5.6760(1)</td>
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<td>(c) ((\AA))</td>
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<td>7.8968(2)</td>
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<td>(\beta) (deg)</td>
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<td>89.916(6)</td>
<td>89.912(6)</td>
<td>89.908(6)</td>
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<td>89.905(6)</td>
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<td>0.5102(4)</td>
<td>0.5106(4)</td>
<td>0.5109(4)</td>
<td>0.5113(4)</td>
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<td>0.2126(6)</td>
<td>0.2131(6)</td>
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</table>

\(^a\)Values are set to zero due to too small magnetic moment below \(T_C\).

in the figure. Compared to the case of \(d_{Co-Ir}\)'s, the volume anomaly and the cooperative movements of oxygen ions are found to be strongly correlated with the ferrimagnetic order. Therefore, the congruent structural anomaly at \(T < T_C\) manifests the ME coupling in \(La_2CoIrO_6\).

According to the mode decomposition analysis on the octahedral distortions (Fig. 8), there exist seven cooperative distortion modes. Among them, only the CBD mode, described in Fig. 1(c), becomes enhanced significantly with magnetic ordering at \(T < T_C\). An order parameter, \((d_{Co-O})^2/(d_{Ir-O})^2\), i.e., the difference between average Co-O and Ir-O bond lengths, is the most relevant to CBD. It is plotted as a function of \(T\) together with the schematic in Fig. 4(a). The correlation of the CBD mode to the magnetic order is scrutinized quantitatively in Fig. 4(b): \(\Delta V\) and \((d_{Co-O})^2/(d_{Ir-O})^2\) are plotted as functions of \(I_{mag}\) of the (100)/(010) reflection.

Both the order parameters show a rough linear relationship with \(I_{mag}\) for lower values of \(I_{mag}\)'s, whereas they seem to increase more rapidly for higher values of \(I_{mag}\)'s. Generally, intensity of magnetic peak is proportional to the squares of the magnetic moment (\(M^2\)). Therefore, the linear relationship to \(I_{mag}\) implies a linear-quadradic ME coupling (order parameters \(-M^2\)). This clearly shows the evidence of magnetoelastic CBD. The coupling constants estimated from the slopes for the low \(I_{mag}\) region are \(\sim +0.002 \AA /\mu_B^2M_{Co}^2\) for \((d_{Co-O})^2/(d_{Ir-O})^2\) and \(\sim +0.008 \AA^3 /\mu_B^2M_{Co}^2\) for \(\Delta V\).

The mechanism of the linear-quadradic magnetoelastic CBD can be demonstrated phenomenologically by the Landau free-energy scheme subject to the magnetic symmetry group. The ferrimagnetic order at \(T < T_C\) breaks the time-reversal symmetry as to lower the magnetic space group from \(P 2_1/n\) to \(P 2_1/1\) (see Table III for comparison of the two groups). The free energy for the ME coupling compatible with the symmetry requirement can be constituted by a power series expansion of representative order parameters multiplied by the magnetic moments of Co and Ir:

\[F_{ME} = a_1(\Delta V_{Co-Ir}^0)M_{Co}M_{Ir} + b_1(\Delta V_{Co-Ir})M_{Co}M_{Ir} + a_2(\Delta V_{Co-Ir}^0)^2(\Delta V_{Co-Ir}) + b_2(\Delta V_{Co-Ir}^0)^2(\Delta V_{Co-Ir})^2 + \ldots,\]

where \(\Delta V_{Co-Ir}^0\) and \(\Delta V_{Co-Ir}\) are \((d_{Co-O})^2/(d_{Ir-O})^2\) and \((d_{Co-O}/d_{Ir-O})^2\) (280 K), respectively, and \(a_1, a_2, b_1, b_2\), etc., are some constant coefficients. The results in Fig. 2 show that

<table>
<thead>
<tr>
<th>Magnetic</th>
<th>1, 2, (-1, ) (m, ) (1, 2, ) (-1, ) (m, ) (1, ) (2, ) (-1, ) (m, ) (1)</th>
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<td>(\Delta d_{Co-Ir}, \Delta d_{Co-Ir}^0)</td>
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<tr>
<td>(2/m)</td>
<td>1 1 1 1 1 1 1 1 1</td>
<td>(M_{Co}, M_{Ir})</td>
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</table>
\[ \Delta_{\text{Co-Ir}} \text{ is negligible compared to } \Delta_{\text{Co/Ir-O}} \text{ (i.e., the CBD mode)} \text{ in } \text{La}_2\text{CoIrO}_6. \text{ Also, the second-order transition with single } T_C \text{ dictates that the magnitude of } M_T \text{ can be presumed to be proportional to that of } M_{\text{Co}} : M_T \approx -\alpha M_{\text{Co}}. \text{ Therefore, the free energy can be simplified as the power series of } M_{\text{Co}}^2 \text{ as}
\]
\[
F_{\text{ME}} = c_1(\Delta_{\text{Co/Ir-O}})M_{\text{Co}}^2 + c_2(\ldots )M_{\text{Co}}^4 + \ldots . \quad (2)
\]

with coefficients \( c_1, c_2, \ldots \). From the condition for minimizing \( F_{\text{ME}} \), it can be shown that \( \Delta_{\text{Co/Ir-O}} \propto M_{\text{Co}}^2 \) roughly. In fact, the linear-quadratic relationship holds in most cases of simple ME coupling. Then the rapid increase of \( \Delta_{\text{Co/Ir-O}} \) shown at high \( I_{\text{mag}} \)’s might reflect the effects of the higher-order terms in \( F_{\text{ME}} \) under strong ME effect.

Despite the significance of the ME effect, multiferroicity could not be induced in the \( \text{La}_2\text{CoIrO}_6 \) double perovskite because of the inversion symmetry of the \( \Gamma_1(A_x) \) magnetic structure. All the components in the ME tensor \( \alpha^T_{ij} \)'s in \( P_i = \alpha^T_{ij}H_j \) (where \( P \) and \( H \) are electric polarization and external magnetic field, respectively) must be zero [45,46]. Also, Song et al. observed no hysteresis of dielectric constant with respect to the applied magnetic field [25], supporting the absence of ferroelectric polarization in the absence of \( H \).

The microscopic origin of the magnetoelastic CBD is unclear at this moment. One plausible explanation can be found in the hybridization mechanism for the spin interactions in double perovskites [14]. According to the hybridization mechanism, preference of the ferromagnetic or antiferromagnetic coupling of spins in adjacent \( B \) and \( B' \) sites can be determined by the virtual spin hopping from the occupied \( B/B' \) orbital to the unoccupied \( B'/B \) orbital through the hybridized orbital states [14]; in the case of \( \text{La}_2\text{CoIrO}_6 \), the occupied orbital is \( \text{Ir} \) (\( j_{\text{eff}} = 1/2 \)) and the unoccupied orbital is \( \text{Co} \downarrow \) [27].

It was shown in Fig. 4 that the CBD was promoted as to decrease (increase) the Ir-O (Co-O) bond length. Such changes in bond lengths can enhance the Co-Ir orbital hybridization via intervening oxygen. Thus, the inter-site spin correlation could be stronger so as to stabilize the ferrimagnetism. (See Ref. [34] for more discussions.) Likewise, the magnetic order can readjust the hybridization strengths as to induce a structural evolution through the spin-orbital-lattice coupling. However, description using the hybridization mechanism might not be reliable for explaining the delicate structural evolution driven by the ME effect. Therefore, more detailed and specific models are needed to fully understand the underlying mechanism of the magnetoelastic CBD.

V. CONCLUSION

We successfully observed the cooperative octahedral distortions and their strong correlation with the ferrimagnetic ordering in \( \text{La}_2\text{CoIrO}_6 \) using ND. The detailed analyses on the CBD showed that the CBD mode evolved with \( T \) being in a linear-quadratic relation with the magnetic moment. This manifests the existence of magnetoelastic CBD in double perovskite.

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APPENDIX A: NEUTRON-DIFFRACTION DATA

The endstation in the SuperHRPD beamline in J-PARC has three detector banks of 30-, 90-, and 172-deg banks. Those detector banks can cover different \( d \) or \( Q \) ranges and their resolutions are different [32,33]. The \( d \) range of the 30-deg bank is as shown in Fig. 5. The magnetic peaks are indexed by magnetic propagation vector \( k = (000) \). The most intense magnetic peak is from (100),(010) reflections (denoted by the asterisk), which were forbidden by \( P2_1/n \) symmetry.

The results of the Rietveld refinement for the ND data taken from the 90-deg bank are listed in Table II. The lattice constants and atomic positions were determined for all the temperatures, while the magnetic moments of Co were determined reliably only at temperatures below 90 K.

APPENDIX B: DETERMINATION OF MAGNETIC MODELS

As shown in Table I, the magnetic representational analysis for the \( P2_1/n \) space group and \( k = (000) \) gives \( \Gamma_{\text{mag}} = 3\Gamma_1(A_x) + 3\Gamma_3(B_x) \) for each of the Wyckoff positions \( 2c(B) \) and \( 2d(B') \) in \( \text{A}_2\text{B}B'O_6 \). We tested \( \Gamma_1(A_x) = (A_1, F_y, A_2) \) and \( \Gamma_3(B_x) = (F_x, A_1, F_y) \) magnetic models for Co sublattices, and the results are shown in Fig. 6. Obviously, the \( \Gamma_1(A_x) \) model fits the intensity of the (100)(010) peak better than the \( \Gamma_3(B_x) \) models. See the contrast in the region denoted by the arrow. This is consistent with the magnetic model \( (A_x, 0, A_z) \) in a previous report [21]. We got the \( F_y \) components additionally. We tested the \( \Gamma_1 \) models with and without the \( b \)-axis moment. The magnetic \( R \) factor \( R_{\text{mag}} \) had a large value (20.4) when the \( b \)-axis moment was set as null. With the \( b \)-axis moment, \( R_{\text{mag}} \) decreased (improved) to 14.5. The magnetic structure in the Ir sublattice was hard to determine due to the small value of the Ir magnetic moment (\( M_{\text{Ir}} \)) as well as the strong neutron absorption.

Based on the \( \Gamma_1(A_x) \) model, we did Rietveld analysis on the 90-deg bank data for both crystal and magnetic structures. The results are summarized in Table II. The \( d \) range and resolution of the 90-deg bank was the most suitable to this paper, considering our sample’s crystallinity and the magnetic peak positions.

Interestingly, it is found that the Co spin direction is confined in the Co-O1-Ir plane as shown in Fig. 7. When viewed in the (a) [110] or (b) [1-10] direction, Co and Ir positions appear to coincide and O1 does to shift from the Co or Ir position as shown in the dotted boxes in Fig. 7. The
O1 displacements can affect both the ferrimagnetic interaction and magnetic anisotropy of the Co ions. The Co spins projected onto the (110) or (1-10) planes are parallel to the directions of the O1 displacements, suggesting that the Co spins are in the Co-O1-Ir planes.

The linear-quadratic relation between the structural order parameters and the values of the magnetic moment was explained in terms of the Landau free energy. The Landau free energy is constituted by a series expansion of the order parameters multiplied by \( M_{\text{Co}} \) or \( M_{\text{Ir}} \), that satisfies the symmetry requirements. The character table for the relevant magnetic groups is shown in Table III. The paramagnetic phase belongs to the \( P_21/n \) magnetic group (with time-reversal symmetry) while the ferrimagnetic phase belongs to \( P_21/n \) (time-reversal symmetry is broken). The point symmetry for \( P_21/n \) is \( 2/m \) and the character value for each of the operations is tabulated. It can be shown easily that \( M_{\text{Co}} \) or \( M_{\text{Ir}} \) can be involved in the Landau free energy only when it is multiplied in the even orders such as in \( M_{\text{Co}}M_{\text{Ir}}, M_{\text{Co}}^2, (M_{\text{Co}}M_{\text{Ir}})^2, \Delta d_{\text{Co/Ir-O1}}M_{\text{Co}}M_{\text{Ir}}, \Delta d_{\text{Co/Ir}}M_{\text{Co}}M_{\text{Ir}}, \text{etc.} \)

**APPENDIX C: DISTORTION MODE DECOMPOSITION**

As shown in Fig. S5 in Ref. [34], the octahedral distortion out of the aristotype \( \text{ABO}_3 \) results in a lowering of crystal symmetry from \( \text{Fm}-3m \) structure to the distorted \( P2_1/n \) structure. Various modes on the octahedral distortions can be involved in the structural distortions. There are seven relevant distortion modes in total: \( \Gamma_1^+(\text{CBD}), \Gamma_3^+(a\text{-type Jahn-Teller}), \Gamma_4^+(a\bar{a}c^0 \text{ in-plane rotation}), \Gamma_5^+(\text{out-of-phase bending}), X_2^+(d\text{-type Jahn-Teller}), X_3^+(a^0 a^0 c^+ \text{ out-of-plane rotation}), \text{and } X_5^+(\text{in-phase tilting}). \) Each of the modes can be decomposed under the frozen phonon scheme in the Bilbao crystallographic server [37,38]. The values of the atomic displacements for each mode are displayed in Fig. 8. The values are also listed in Table S1 in Ref. [34].

The significance of each mode can be represented by the values of the atomic displacements in angstroms. It is shown for all \( T, \Gamma_4^+, X_3^+, \text{ and } X_5^+ \) that distortion modes are dominant with high values of atomic displacements. This reflects the prevalence of the three distortions in \( \text{La}_2\text{CoIrO}_6 \). However, the amplitudes of the three distortion modes seem robust upon the \( T \) changes, implying they are less relevant to the ME effect.
On the other hand, $\Gamma_1^+$ and $\Gamma_5^+$ modes show strong anomalies at $T_s$’s below 100 K; the two types of distortions become enhanced significantly at the low $T_s$’s. The $\Gamma_1^+$ mode represents the isotropic expansion or shrinkage of the octahedral, i.e., the CBD mode. Since it shows the strongest $T$ anomaly among the seven distortion modes, we can tell the magnetic order mainly induces the octahedral distortions mostly following the symmetry of the $\Gamma_1^+$ mode. This confirms that the CBD is associated with the magnetic order and, therefore, manifests the magnetoelastic CBD in La$_2$CoIrO$_6$.

[44] Debye-Grüneisen model for volume is $V = V_{0,0} (1 + \frac{\varepsilon (T)}{Q - bE_T})$. We employed the values of $V_{0,0}$ = 249,694 K, $\theta_{Debye}$ = 457 K, $Q$ = $4.6 \times 10^{-17}$ J, and $b$ = 1.5.