

Phase locking the spin precession in a storage ring

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This letter reports the successful use of feedback from a spin polarization measurement to the revolution frequency of a 0.97 GeV/c bunched and polarized deuteron beam in the Cooler Synchrotron (COSY) storage ring in order to control both the precession rate (≈ 121 kHz) and the phase of the horizontal polarization component. Real time synchronization with a radio frequency (rf) solenoid made possible the rotation of the polarization out of the horizontal plane, yielding a demonstration of the feedback method to manipulate the polarization. In particular, the rotation rate shows a sinusoidal function of the horizontal polarization phase (relative to the rf solenoid), which was controlled to within a one standard deviation range of $\sigma = 0.21$ rad. The minimum possible adjustment was 3.7 mHz out of a revolution frequency of 753 kHz, which changes the precession rate by 26 mrad/s. Such a capability meets a requirement for the use of storage rings to look for an intrinsic electric dipole moment of charged particles.

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During the past years, the importance of polarized beams has been demonstrated in numerous experiments

at colliders as well as at storage rings such as the Cooler Synchrotron COSY. Recently the emphasis of such ex-

periments has started to shift from nuclear and hadron physics to precision measurements. This letter describes the successful effort to use measurements of the polarization of a storage ring deuteron beam in a feedback loop to control in real time the rate of precession in the horizontal (ring) plane and the phase of that rotating polarization relative to an external reference. This work was carried out in the context of the effort to search for an intrinsic electric dipole moment (EDM) of charged particles circulating in the ring [1].

An EDM aligned along the particle spin axis is CP-violating and any observation of such a moment would be a signal of new physical processes possibly related to the matter-antimatter asymmetry of the universe [2, 3]. An EDM may be observed by measuring the rate of spin precession in an external electric field. For charged particles, confinement in a storage ring exposes them to the particle rest frame electric field that closes the storage ring orbit. To work best for small EDMs, the beam polarization should begin parallel to the particle velocity (and perpendicular to the radial electric field) and precess, due to the EDM, into the vertical direction where that spin component is stable and may be measured in a scattering experiment. Since the precession due to the magnetic moment of a particle is different in electric and magnetic fields (compared to the amount by which the particle path is bent), some combination of E and B bending field may be found that allows the reference particle to travel in a “frozen spin” configuration in which the polarization and the velocity remain aligned. But maintaining this alignment over a thousand seconds [4] for a statistically significant measurement requires control of the rotation rate at the level of parts per billion; hence real time feedback from a continuously running polarization measurement (available at high precision [5]) is mandatory for any such EDM experiment.

The frozen spin configuration is not the only possibility to observe an EDM. It has been proposed that precession of the EDM may be achieved through the use of an rf Wien filter with a vertical magnetic field [6, 7] operating at a harmonic frequency of the horizontal polarization precession in the plane of a pure magnetic storage ring. In this case both the precession rate and phase relative to the Wien filter rf must be controlled. Here, we report on the first successful installation and operation of a feedback system fulfilling these requirements.

The measurements presented here were performed at the Cooler Synchrotron COSY at the Forschungszentrum Jülich [8]. A vector polarized deuteron beam was injected at time $t = 0$ and accelerated to a momentum of 970 MeV/ c . The beam intensity was approximately 10^9 deuterons per fill. The vector polarization was perpendicular to the ring plane and was alternated from cycle to cycle from upward to downward direction. The corresponding values for the polarization were $p^{\text{up}} = 0.30 \pm 0.03$ and $p^{\text{down}} = -0.46 \pm 0.03$. After acceleration the beam was

electron-cooled for 74 s to reduce the beam emittance. A radio-frequency (rf) cavity to bunch the beam was used throughout the 200 s long cycle. Starting at $t = 80$ s the beam was slowly extracted onto an internal carbon target by applying a white noise electric field. Elastically scattered deuterons were detected in scintillation detectors consisting of rings and bars around the beam pipe. The detector covers a range from 9 to 13 degrees in polar angle and is segmented in four regions in the azimuthal angle (up, down, left and right). The elasticity of the event was guaranteed by stopping the deuterons in the outer scintillator ring and measuring their energy deposition [9]. The left-right asymmetry gives access to the vertical polarization, the up-down asymmetry is sensitive to the polarization perpendicular to the momentum vector in the horizontal plane of the ring. At $t = 85$ s an rf solenoid was used to rotate the polarization from the initially vertical direction into the horizontal plane.

Once the spin is rotated out of the vertical direction, its horizontal component starts to precess around the vertical axis. Defining the spin motion in the rest frame of the particle, the precession frequency is

$$f_s = \nu_s f_{\text{cosy}} = \gamma G f_{\text{cosy}}, \quad (1)$$

where $\nu_s = \gamma G \approx -0.16$ is the spin tune, γ the Lorentz factor, G the gyromagnetic anomaly and f_{cosy} the revolution frequency. Note that the sign of f_s indicates the direction of the spin rotation. In order to rotate the polarization vector effectively, the rf solenoid has to run at a resonance frequency, which is given as

$$f_{\text{rf}} = (k + \nu_s) f_{\text{cosy}}, k \in \mathbb{Z}. \quad (2)$$

For this experiment the solenoid was operated at $|f_{\text{rf}}| \approx 873$ kHz ($k = -1$). Table I summarizes the most important parameters of the experiment.

In the further course of the cycle the solenoid was also used to restore the vertical polarization providing a test for the feedback system. As the solenoid field only acts on the sideways component of the polarization its effective strength is largest if the maximum of the rf solenoid field coincides in time with the horizontal polarization being sideways and vanishes if both are parallel. The build-up of vertical polarization is thus proportional to $\sin \phi$, where ϕ is the relative phase between the rf frequency and the spin precession at the location of the rf solenoid. $\phi = 0$ corresponds to the case where the polarization vector is parallel to the magnetic field of the solenoid when it is at its maximum value. The slope of the polarization build-up as a function of ϕ is thus a measure how well the relative phase between the two is under control. For this, the solenoid was again switched on at $t = 115$ s at low field strength.

In general, the relative phase ϕ between the rf frequency and the spin precession frequency is time dependent and defined as

$$\phi(t) = 2\pi(t - t_0)(f_{\text{rf}} - \nu_s f_{\text{cosy}}) + \phi_0, \quad (3)$$

deuteron momentum p	0.970 GeV/c
rel. velocity β	0.459
Lorentz factor γ	1.126
slip factor η	-0.58
gyromagnetic anomaly G	≈ -0.143
revolution frequency f_{cosy}	752543 Hz
precession frequency $ f_s $	121173 Hz
resonance frequency $ f_{\text{rf}} $	873716 Hz
cycle length	200 s

TABLE I. Parameters of the experiment.

where t is the time in the cycle, t_0 is the time the measurement starts and ϕ_0 is the phase at $t = t_0$. As the solenoid is located at a fixed position in the ring, the time is sampled as $t - t_0 = n/f_{\text{cosy}}$ where n denotes the turn number:

$$\phi(n) = 2\pi n \left(\frac{f_{\text{rf}}}{f_{\text{cosy}}} - \nu_s \right) + \phi_0. \quad (4)$$

As long as Eq. (2) is fulfilled, $\phi(n)$ will remain constant (modulo 2π), since the term in the parentheses is an integer. However, even for a small mismatch between the resonance frequency and f_{rf} , the value of ϕ will continuously change and the polarization build-up will be diminished or even canceled. If one accepts the build-up to drop to 80% at the end of a 1000s cycle (corresponding to $\cos \Delta\phi = 0.8$ and $\Delta\phi \approx 0.65$ rad), both frequencies have to be adjusted with a precision better than $\Delta f/f = 10^{-10}$. As discussed in Ref. [5], both the reproducibility and the stability of the spin tune ν_s are in the order of 10^{-8} to 10^{-9} . Figure 1(a) provides an example for the variation of ϕ over one cycle without a feedback system. Starting at an arbitrary value the phase is continuously changing over the whole cycle. With the same initial settings other cycles show both weaker and stronger time dependencies. Therefore, an active feedback system is essential to keep ϕ within the desired interval of $\pm\Delta\phi$.

The basic principle of the feedback system is to control the spin precession frequency by varying f_{cosy} and to match its phase to the radio frequency of the solenoid. Figure 2 illustrates schematically the feedback control loop. In a first step, the phase of the spin precession is measured using a polarimeter and a stand-alone data acquisition system as described in [5]. Then, the relative phase $\phi_{\text{meas}} = \phi + \phi_{\text{det}}$ is determined, which corresponds to the difference between the solenoid phase and the spin precession phase. Both phases are measured using the same reference clock. The additional constant offset ϕ_{det} originates from the relative position of polarimeter and rf solenoid in the ring and from cable delays. The typical measurement period for each data point is about 2s depending on the available intensity of the beam, which is continuously extracted onto the target during the cycle.

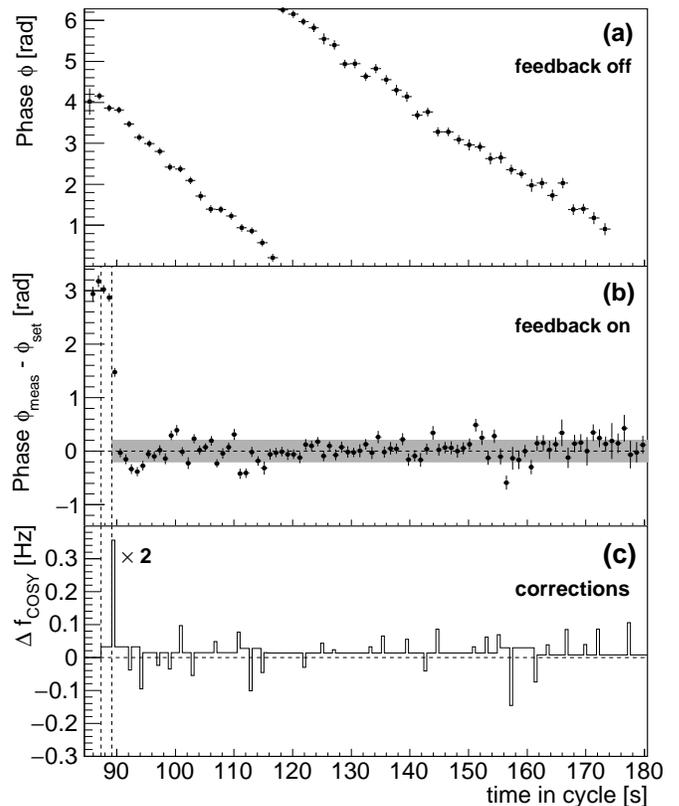


FIG. 1. Phase between the measured spin direction and the rf frequency of the solenoid (a) without and (b) with an active feedback system. The y-axis in (b) has been shifted to the predefined value. The grey band indicates the $\pm 1\sigma$ band for the resulting phase distribution. In (c) the corresponding corrections to the synchrotron frequency are illustrated.

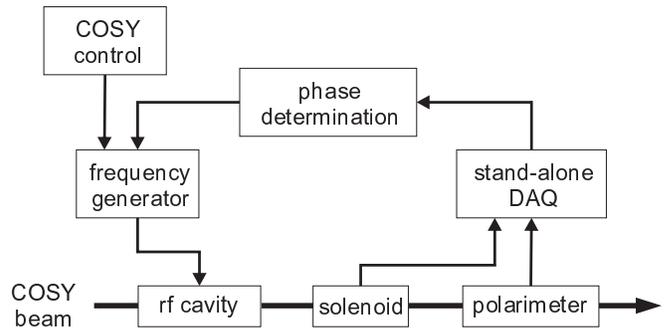


FIG. 2. Schematic layout of the feedback system. Based on the measured spin direction in the polarimeter and the phase of the rf solenoid the control system adds an offset in the range of ± 2 Hz to the nominal value for the synchrotron frequency. The minimum step size is 3.7 mHz.

The purpose of the feedback is twofold: First, the phase has to be adjusted to a predefined value ϕ_{set} to define and to reproduce the experimental conditions. This is done by running off-resonance for a short period of time (in the order of 100ms, e.g. in Fig. 1(b) at $t \approx 90$ s) until the desired phase has been reached. It is also used

to compensate larger deviations during the course of the cycle. Second, the resonance condition, defined in Eq. (2) has to be fulfilled in order to keep ϕ_{meas} constant. This is achieved by introducing a corresponding offset to the synchrotron frequency.

The necessary frequency change Δf_{cosy} can be calculated using the derivative of Eq. (4):

$$\frac{\partial \phi}{\partial f_{\text{cosy}}} = 2\pi n \left(-\frac{f_{\text{rf}}}{f_{\text{cosy}}^2} - \frac{\partial \nu_s}{\partial f_{\text{cosy}}} \right). \quad (5)$$

While the first term originates from the different arrival time at the solenoid, the second term describes the change of the spin tune:

$$\frac{\Delta \nu_s}{\nu_s} = \frac{\Delta \gamma}{\gamma} = \beta^2 \frac{\Delta p}{p} = \frac{\beta^2}{\eta} \frac{\Delta f_{\text{cosy}}}{f_{\text{cosy}}}, \quad (6)$$

where β is the particle velocity and η the so-called slip factor, which connects a change in momentum p into a change in revolution frequency. Using values given in Tab. 1 one obtains

$$\Delta \phi \approx 6.93 \frac{\text{rad}}{\text{Hz s}} \Delta f_{\text{cosy}} \Delta t. \quad (7)$$

With a minimum step size of 3.7 mHz offered by the standard COSY frequency generator it was possible to induce phase adjustments in steps of $\Delta \phi \approx \pm 26$ mrad/s.

Figure 1(b) shows the phase difference $\phi_{\text{meas}} - \phi_{\text{set}}$ versus time while the feedback system was active. In Fig. 1(c) the changes to the synchrotron frequency are illustrated. The feedback system started monitoring the phase at $t = 85$ s when the polarization vector was turned into the horizontal plane. While a first correction of the phase drift was applied at the first vertical dashed line, the pulse at the second dashed line was moving the phase to the predefined value ϕ_{set} . Once this phase had been reached it was kept stable over the remaining cycle. The resulting phase distribution has a width of $\sigma = 0.21$ rad, indicated by the shaded band in Fig. 1b, which is well below the allowed variation defined by $\cos \Delta \phi = 0.8$.

Fig. 1(b) already proves the functionality of the feedback system. In order to confirm that the relative phase can really be set to an arbitrary value between 0 and 2π , the phase dependent build-up of the vertical polarization was measured. The basic principle of the experiment is shown in Fig. 3.

Once the polarization vector had been turned into the horizontal plane (first vertical dashed line), the feedback system was switched on, maintaining the relative phase ϕ_{meas} at a predefined value $\phi_{\text{set}} = 0.5\pi$. At $t = 115$ s (second dashed line) the solenoid was switched back on at a reduced strength causing the polarization to rotate slowly out of the horizontal plane — either upwards or downwards depending on the selected value of $\phi = \phi_{\text{set}} - \phi_{\text{det}}$. The field integral $\int B_{\text{eff}} dl$ of the solenoid was about $4.6 \cdot 10^{-4}$ Tmm. This corresponds to a maximal polarization rotation of 50 mrad/s.

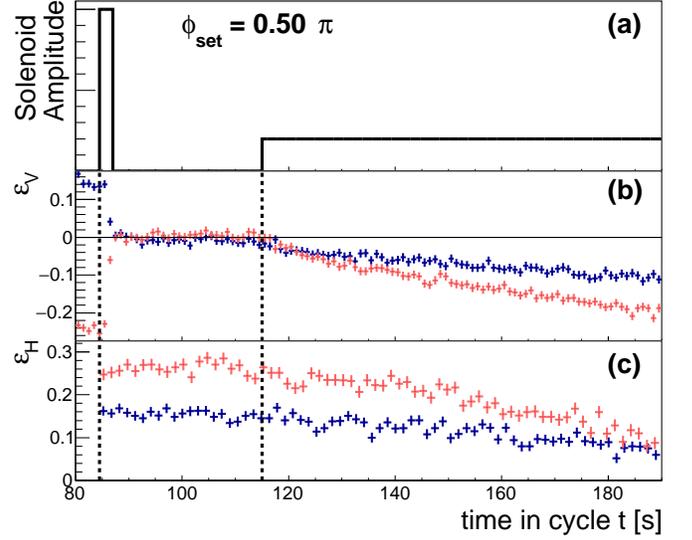


FIG. 3. Vertical (ϵ_V) and horizontal (ϵ_H) asymmetries for positive (blue) and negative (red) initial polarization. The polarization is rotated into the horizontal plane by means of the solenoid at $t = 85$ s. The feedback system is switched on and the polarization is slowly rotated back towards the

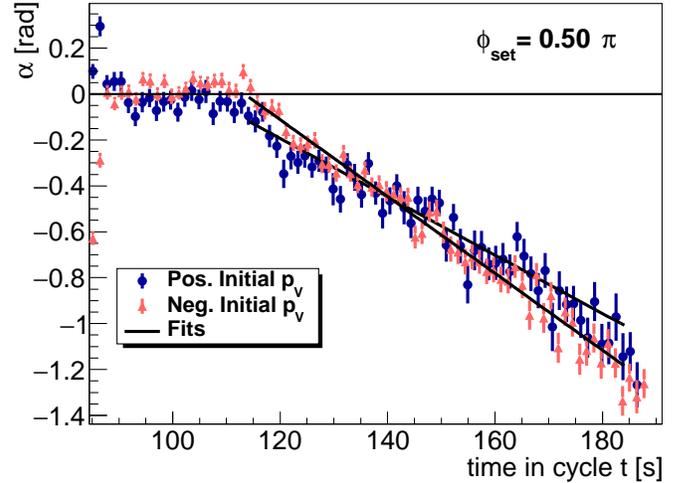


FIG. 4. Rotation angle α as function of time since injection for positive (blue, circles) and negative (red, triangles) initial polarization.

Figure 3(a) qualitatively shows the amplitude of the solenoid. Figure 3(b) shows the asymmetry from the counting rates in the left (N_L) and right (N_R) detector segments $\epsilon_V = (N_L - N_R)/(N_L + N_R)$ proportional to the polarization in the vertical direction. Figure 3(c) shows the asymmetry ϵ_H proportional to the amplitude of the polarization in the horizontal plane. ϵ_H is obtained from the oscillating event rates in the upper and lower segment of the detector, N_U and N_D as described in Ref. [5].

The spin rotation is analyzed by examining the angle $\alpha = \arctan(\epsilon_V/\epsilon_H)$ between the polarization vector and

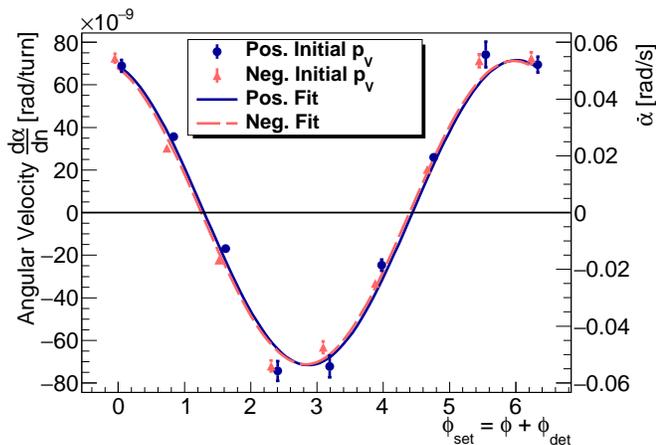


FIG. 5. Angular velocity of the solenoid spin rotation as a function of the nominal phase for data with positive (blue, circles) and negative (red, triangles) initial polarization. For better visibility the points were slightly shifted to the left and right horizontally.

the horizontal plane. α is independent on the initial degree of polarization and is expected to either increase or decrease linearly with a slope proportional to $\sin \phi$. Figure 4 shows α as function of time in cycle for $\phi_{\text{set}} = 0.5 \pi$. Both initial polarization states show a similar slope. Figure 5 shows the fitted slopes as a function of the nominal phase $\phi_{\text{set}} = \phi + \phi_{\text{det}}$. The build-up proportional to $\sin \phi$ is another striking proof that the method works.

In conclusion, we have shown that the high precision measurement of the spin tune, discussed in [5], can be used to perform a real-time measurement of the relative phase between the spin precession and an external radio frequency device. This has been used for the first time to implement an active feedback system to stabilize this phase at a level of 0.21 rad and to reproduce the phase dependence of the spin rotation in an rf solenoid. As the sensitivity to phase variations is the same for the rf Wien filter, this is an essential prerequisite towards the first measurement of an EDM in a storage ring. In addition, such a feedback system can also be used in the frozen spin method [10], where the polarization has to be kept aligned to the momentum vector in the horizontal plane.

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